

$$\sin x - \sin 15x \cos x = 3/2$$

подсказка

$$A \sin x + B \cos x = 3/2$$

$$A=1 \quad B=-\sin 15x$$

$$\sqrt{1+\sin^2 15x}(\sin x (1/\sqrt{1+\sin^2 15x}) + \cos x * (-\sin 15x/(1+\sin^2 15x)) = 3/2$$

$$\sqrt{1+\sin^2 15x} \sin(x+t) = 3/2$$

$$\max(\sqrt{1+\sin^2 15x} \sin(x+t)) = \sqrt{2} = 1.4... < 3/2$$

$$\cos t = 1/\sqrt{1+\sin^2 15x}$$

$$t = \arccos(1/\sqrt{1+\sin^2 15x})$$

$$t = -\arccos(1/\sqrt{1+\sin^2 15x})$$

$$\sin t = -\sin 15x/(1+\sin^2 15x)$$

$$t = \arcsin(-\sin 15x/(1+\sin^2 15x))$$

$$t = P - \arcsin(-\sin 15x/(1+\sin^2 15x))$$

Ответ: решений нет

$$\begin{aligned}\sin 3x - 2\sin 18x \sin x &= 3\sqrt{2} - \cos 3x + 2\cos x \\ \sin 3x + \cos 3x &= 3\sqrt{2} + 2\sin 18x \sin x + 2\cos x\end{aligned}$$

$$\begin{aligned}\sqrt{2} \sin(P/4+3x) &= 3\sqrt{2} + \sqrt{4+4\sin^2 18x} \sin(x+t) \\ \sqrt{2} \sin(P/4+3x) &= 3\sqrt{2} + 2\sqrt{1+\sin^2 18x} \sin(x+t)\end{aligned}$$

$$\begin{aligned}\sqrt{2} \sin(P/4+3x) &= \sqrt{2} \\ \sin(P/4+3x) &= 1 \\ P/4+3x &= P/2 + 2Pk \\ 3x &= P/4 + 2Pk \\ x &= P/12 + 2Pk/3 \\ 2\sqrt{1+\sin^2 18x} \sin(x+t) &= -2\sqrt{2}\end{aligned}$$

$$\begin{aligned}\cos t &= 2\sin 18x / \sqrt{4+4\sin^2 18x} \\ \sin t &= 2 / \sqrt{4+4\sin^2 18x}\end{aligned}$$

$$1) x = P/12 \\ \cos t = (2\sin 3P/2) / \sqrt{4+4\sin^2 3P/2}$$

$$\cos t = -2/2\sqrt{2}$$

$$\cos t = -\sqrt{2}/2$$

$$\sin t = 2 / \sqrt{4+4\sin^2 3P/2}$$

$$\sin t = \sqrt{2}/2$$

$$t = 3P/4$$

$$2\sqrt{2} \sin(5P/6) = -2\sqrt{2}$$

$$\sin(5P/6) = -1 \quad \text{--- не подходит}$$

$$2) x = 3P/4$$

$$\cos t = 2\sin 27P/2 / \sqrt{4+4\sin^2 27P/2}$$

$$\cos t = 2\sin 27P/2 / \sqrt{4+4\sin^2 3P/2}$$

$$\cos t = 2\sin 3P/2 / \sqrt{4+4\sin^2 3P/2}$$

$$\cos t = -\sqrt{2}/2$$

$$\sin t = 2 / \sqrt{4+4\sin^2 18x}$$

$$\sin t = 2 / \sqrt{4+4\sin^2 3P/2}$$

$$\sin t = \sqrt{2}/2$$

$$t = 3P/4$$

$$2\sqrt{1+\sin^2 18x} \sin(x+t) = -2\sqrt{2}$$

$$2\sqrt{1+\sin^2 3P/2} \sin(3P/2 + 3P/4) = -2\sqrt{2}$$

$$\sin(3P/2 + 3P/4) = -1 \quad \text{--- не подходит}$$

$$3) x = 17P/12$$

$$\cos t = 2\sin 18x / \sqrt{4+4\sin^2 18x}$$

$$\sin t = 2 / \sqrt{4+4\sin^2 18x}$$

$$\cos t = 2\sin 3P/2 / \sqrt{4+4\sin^2 3P/2}$$

$$\cos t = -\sqrt{2}/2$$

$$\sin t = 2 / \sqrt{4+4\sin^2 3P/2}$$

$$\sin t = \sqrt{2}/2$$

$$t = 3P/4$$

$$2\sqrt{1+\sin^2 3P/2} \sin(26P/12) = -2\sqrt{2}$$

$$2\sqrt{1+\sin^2 3P/2} \sin P/6 = -2\sqrt{2}$$

$$\sin P/6 = -1 \quad \text{--- не подходит}$$

